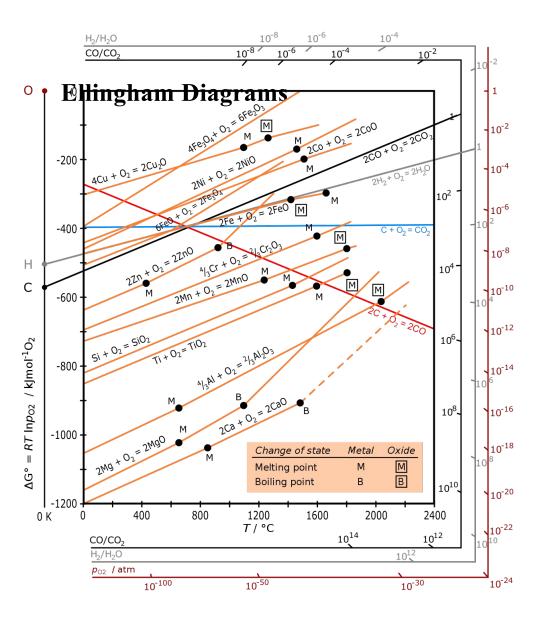
Dependencies of the Heat of Formation

Reference State: Elemental ground state at STP has an enthalpy of formation of 0 N_2 , O_2 , He etc.

		$\Delta H_{f,298.15}$	$\Delta G_{f,298.15}$	Heat Capacity Constants			
		kJ/mol	kJ/mol	A	В	С	D
Solid	ls: Standard state is p	ure solid at	298.15 K,	l bar.			
	Carbon (graphite) (298-1300 K)	0	0	-3.958	5.586E-02	-4.548E-05	1.517E-08
	Calcium carbonate, CaCO ₃	-1206.92	-1128.79				
	Calcium oxide, CaO	-635.09	-604.03				
	Glucose	-1273.3	-908.1				
Misc	ellaneous Gases						
899	Nitrous oxide	82.05	103.638	21.62	0.07281	-5.778E-05	1.830E-08
901	Oxygen	0	0	28.11	-3.7E-06	1.746E-05	-1.065E-08
902	Hydrogen (equilibrium)	0	0	27.14	0.009274	-1.381E-05	7.645E-09
905	Nitrogen	0	0	31.15	-0.01357	2.680E-05	-1.168E-08
908	Carbon monoxide	-110.53	-137.16	30.87	-0.01285	2.789E-05	-1.272E-08
910	Sulfur dioxide	-296.81	-300.14	23.85	0.06699	-4.961E-05	1.328E-08
911	Sulfur trioxide	-396.0	-371.3	19.21	0.1374	-1.176E-04	3.700E-08
912	Nitric oxide	90.25	86.58	29.35	-0.00094	9.747E-06	-4.187E-09
913	Helium-4	0	0	20.8			
914	Argon	0	0	20.8			
917	Fluorine	0	0				
918	Chlorine	0	0	26.93	0.03384	-3.869E-05	1.547E-08
919	Neon	0	0	20.8			
920	Krypton	0	0	20.8			
922	Bromine	0	0	33.86	0.01125	-1.192E-05	4.534E-09
959	Xenon	0	0	20.8			

Generally, energy is released on formation of a molecule from the elements if the molecule is stable, so the heat of formation is generally negative. For unstable molecules such as NO which is a radical formed at high temperatures, the heat of formation is positive (endothermic).



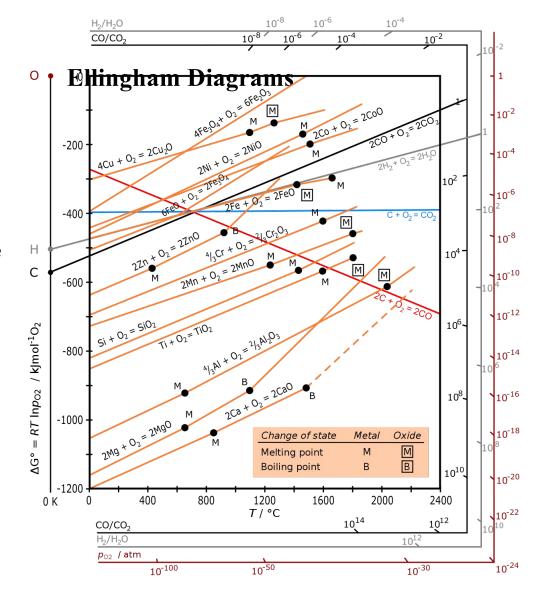
For a reaction $\Delta G = \Delta H - T \Delta S$

Gas has more entropy than solid

 Δ H positive, Δ S negative if moles of gas decrease A line in Δ G vs T plot with positive slope

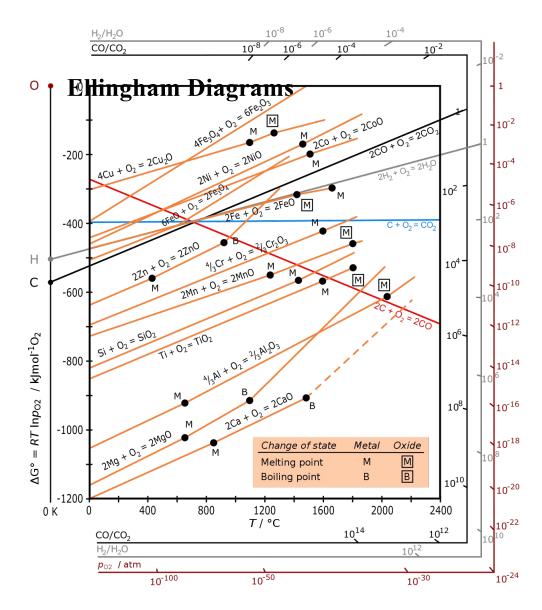
Reactions that increase the moles of gas have negative slope

No change in moles of gas a flat slope



 p_{O2} is 1 atm Reactions with one mole of O_2

- Determine the relative ease of reducing a given metallic oxide to metal
- 2. Determine the partial pressure of oxygen that is in equilibrium with a metal oxide at a given temperature
- 3. Determine the ratio of carbon monoxide to carbon dioxide that will be able to reduce the oxide to metal at a given temperature.



4

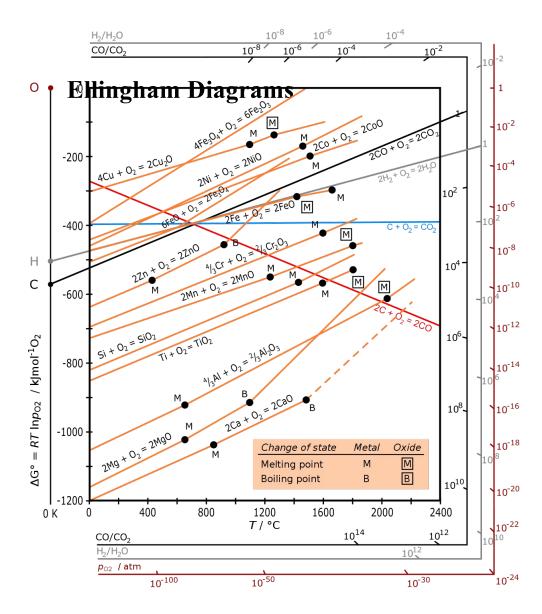
1. Ease of Reduction

Top are most easily reduced

If the curve is below, it will drive the higher curve to reduction (reverse)

High temperatures are needed to reduce iron oxide with carbon (coke)

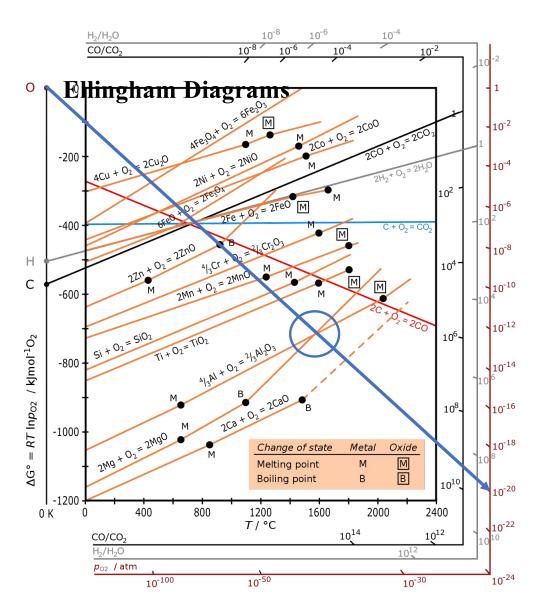
Magnesothermal reduction, use magnesium metal to reduce titania or silica to titanium metal or silica metal



2. Equilibrium O₂ Partial Pressure

Red P_{O2} scale

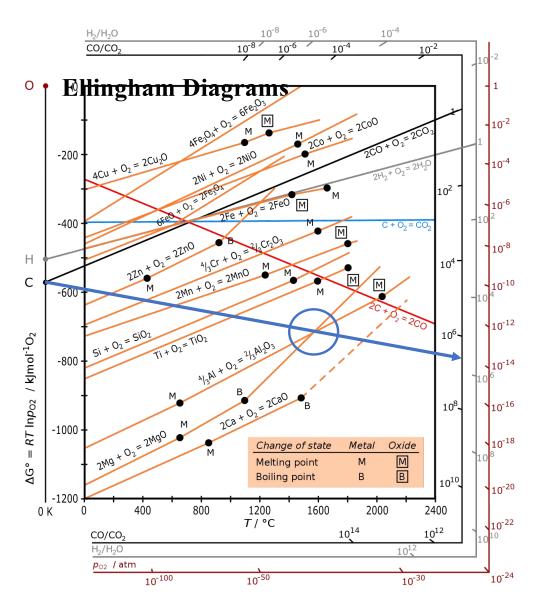
Partial pressure of 10⁻²⁰ atm of O₂
Above will oxidize aluminum at 1600°C below will reduce



3. Ratio of CO/CO₂ Needed for Reduction with Carbon

To reduce an oxide, you need a minimum CO/CO₂ ratio

To reduce Al at 1600°C you need a CO/CO₂ ratio greater than 5x10⁷



Ellingham Diagrams

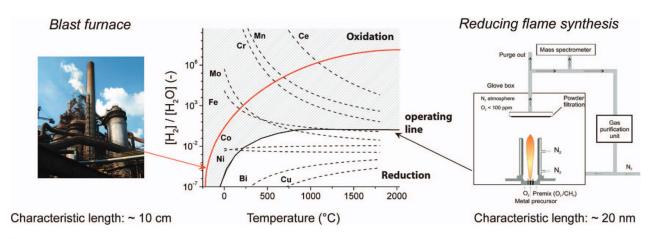


FIG. 5. Thermodynamic calculations in the form of an Ellingham diagram allow discussions on accessible alloys and metals. The lines which lie below the flame process operating line indicate accessible metals at the corresponding temperature (copper, cobalt, nickel, and iron above 1500°C). Others, such as cerium, manganese are not accessible in the current CO/H₂ system.

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Chemical Aerosol Engineering as a Novel Tool for Material Science: From Oxides to Salt and Metal Nanoparticles

Evagelos K. Athanassiou, Robert N. Grass, and Wendelin J. Stark

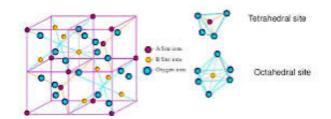
Institute for Chemical and Bioengineering, ETH Zurich, Zurich, Switzerland

Relative magnitude of heat of formation from elements, oxides, heat of fusion, heat of transition

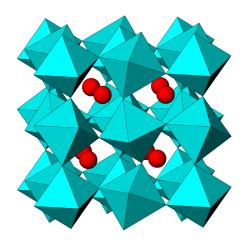
Table 7.1 Magnitudes of enthalpies of various reactions of a ternary oxide using Mg₂SiO₄ as an example (after Navrotsky [1]).

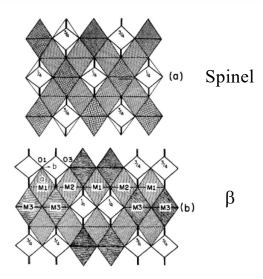
$2Mg(s) + Si(s) + 2O_2(g) = Mg_2SiO_4$ (olivine)	-2170.41 kJ mol-1
$2MgO + SiO_2(s) = Mg_2SiO_4$ (olivine)	-56.61 kJ mol-1
Mg_2SiO_4 (olivine) = Mg_2SiO_4 (liq.)	114 kJ mol-1
Mg_2SiO_4 (olivine) = Mg_2SiO_4 (β)	29.9 kJ mol-1
$Mg_2SiO_4(\beta) = Mg_2SiO_4$ (spinel)	9.1 kJ mol ⁻¹

Crystal structure of Spinel Ferrite

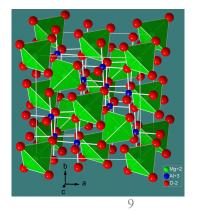


Olivine





Spinel



Heats of formation for various titanium oxides

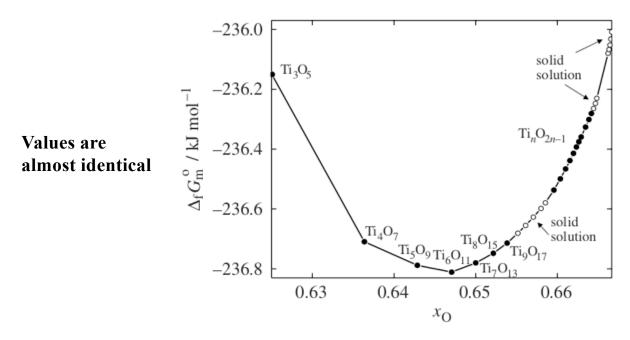
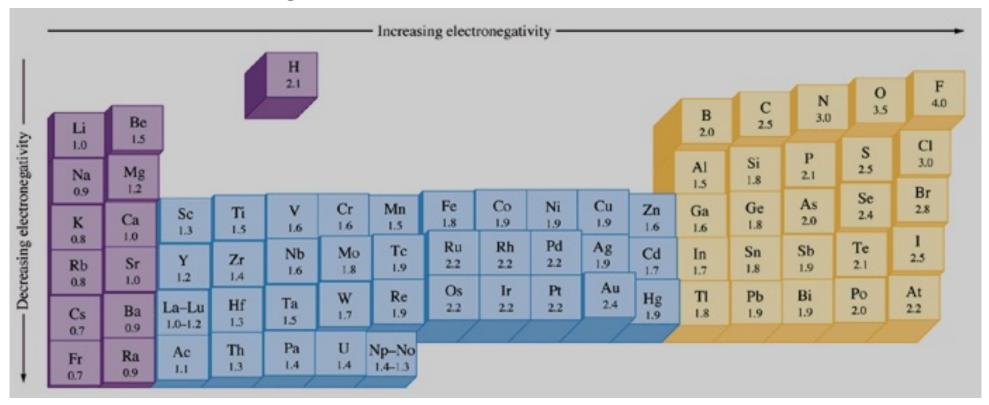


Figure 7.1 The Gibbs energies of formation of stoichiometric and non-stoichiometric compounds in the system Ti_3O_5 – TiO_2 [4]. Composition given as mole fraction O.

Electronegativity, the ability of an atom to attract electrons in a bond Linus Pauling



Factors involved in the heat of formation: electronegativity and atomic size

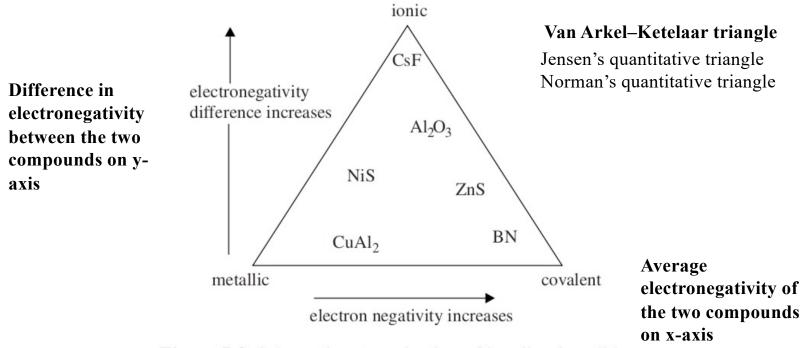


Figure 7.2 Schematic categorization of bonding in solids.

Energetics of compound formation

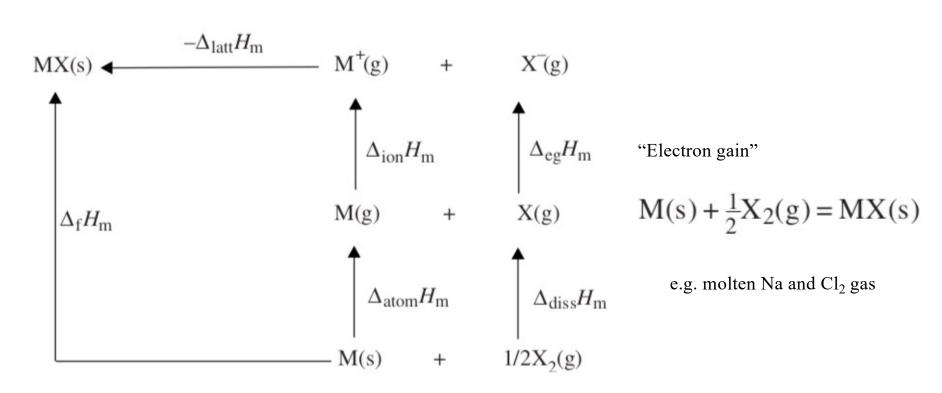


Figure 7.3 Thermodynamic cycle for the formation of MX(s).

Energetics of compound formation

$$M(s) + \frac{1}{2}X_{2}(g) = MX(s)$$

$$M^{+}(g) + X^{-}(g) = MX(s)$$

$$M^{+}(g) + X^{-}(g) = MX(s)$$

$$M^{+}(g) + X^{-}(g) = MX(s)$$

$$M(s) = M(g)$$

$$\Delta_{atom}H_{m}$$

Figure 7.3 Thermodynamic cycle for the formation of
$$MX(s)$$
.

$$X(g) + e^{-} = X^{-}(g) \qquad \Delta_{eg}H_{m}$$

$$\Delta_{f}H_{m}(MX) = -\Delta_{latt}H_{m} + \Delta_{atom}H_{m} + \Delta_{ion}H_{m} + \Delta_{diss}H_{m} + \Delta_{eg}H_{m}$$

Energetics of compound formation

$$M^+(g) + X^-(g) = MX(s)$$
 $-\Delta_{latt}H_m$

$$\Delta_{\text{latt}} H_{\text{m}} = \Phi_{\text{electrostatic}} + \Phi_{\text{repulsion}} + \Phi_{\text{dispersion}} + \Phi_{\text{polarization}} + \Phi_{\text{crystal field}}$$

Electron electron repulsion

Van der Waals or dispersion (d+ makes d- leads to net attraction)

Polarization (shifting within compound of electrons)

Crystal field effects

$$\begin{split} \Delta_{\text{latt}} H_{\text{m}} &= \varPhi_{\text{electrostatic}} + \varPhi_{\text{repulsion}} + \varPhi_{\text{dispersion}} + \varPhi_{\text{polarization}} \\ &+ \varPhi_{\text{crystal field}} \end{split}$$

Electrostatic interactions in NaCl

$$6\frac{e^2 q_{\rm M} q_{\rm X}}{r_{\rm MX}}$$

Nearest neighbors of Na⁺ and Cl₋

$$-12\frac{e^2q_{\rm M}q_{\rm X}}{\sqrt{2}r_{\rm MX}}$$

Repulsive cationic terms, second nearest neighbors

$$8\frac{e^2 q_{\rm M} q_{\rm X}}{\sqrt{3} r_{\rm MX}}$$

Third nearest neighbors, attraction between M^+ and X^-

Generally:

$$\Phi = \frac{e^2 q_{\rm M} q_{\rm X}}{r_{\rm MX}} \left(6 - \frac{12}{\sqrt{2}} + \frac{8}{\sqrt{3}} - \frac{6}{\sqrt{4}} + \cdots \right)$$

$$\Phi_{\text{electrostatic}} = \frac{NMe^2 q_{\text{M}} q_{\text{X}}}{r_{\text{MX}}}$$
M is the Madelung constant

$$\Delta_{\rm latt} H_{\rm m} = \varPhi_{\rm electrostatic} + \varPhi_{\rm repulsion} + \varPhi_{\rm dispersion} + \varPhi_{\rm polarization} \\ + \varPhi_{\rm crystal \, field}$$

Repulsion and Dispersion Terms

Leonard-Jones (6-12) Potential

$$V_{
m LJ}(r)=rac{A}{r^{12}}-rac{B}{r^6}$$

 $V_{\rm LJ}(r) = \frac{A}{r^{12}} - \frac{B}{r^6}$ 12 is repulsive since dE/dr = F is positive (guessed) 6 is van der Waals attractive force (calculated)

Buckingham Potential

$$\Phi_{12}(r)=A\exp(-Br)-rac{C}{r^6}$$

Exponential term works better for ceramics

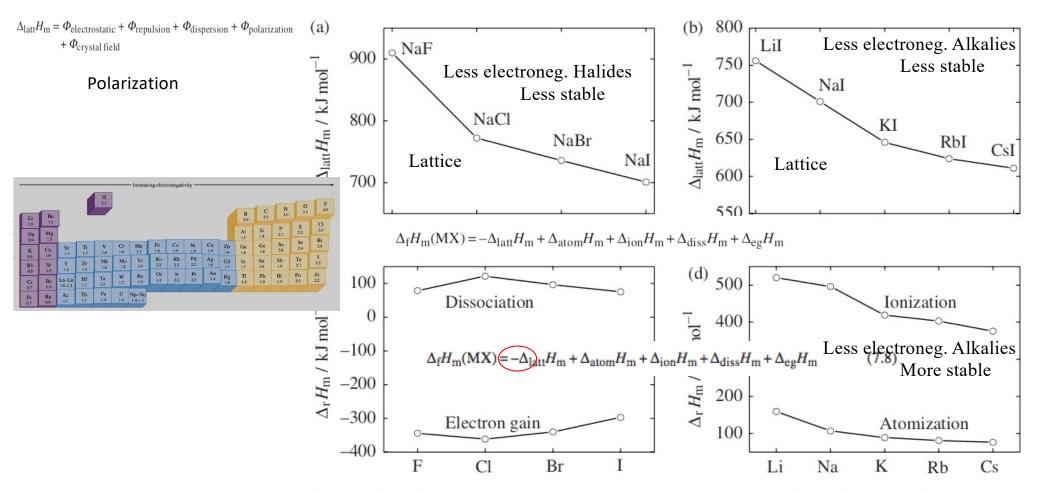


Figure 7.4 Thermodynamic data needed in evaluation of the enthalpy of formation of MX(s). (a) Lattice enthalpy of sodium halides; (b) lattice enthalpy of alkali iodides; (c) electron gain and dissociation enthalpies of halides; (d) ionization and atomization enthalpies of alkali metals.

Trends in Enthalpy of Formation Alkali

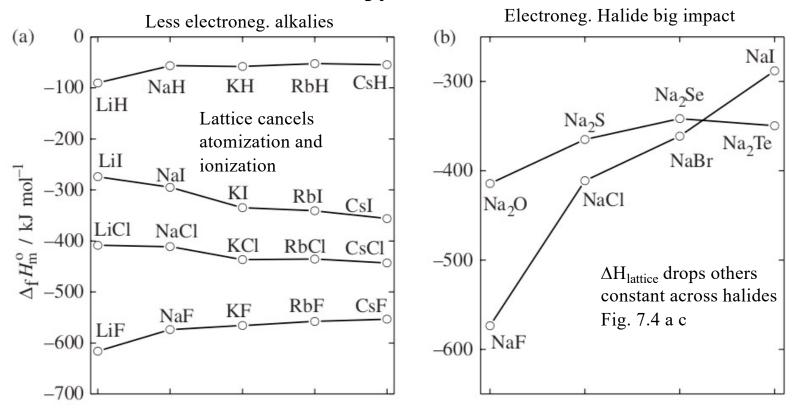


Figure 7.5 Enthalpy of formation of binary compounds of the alkali metals.

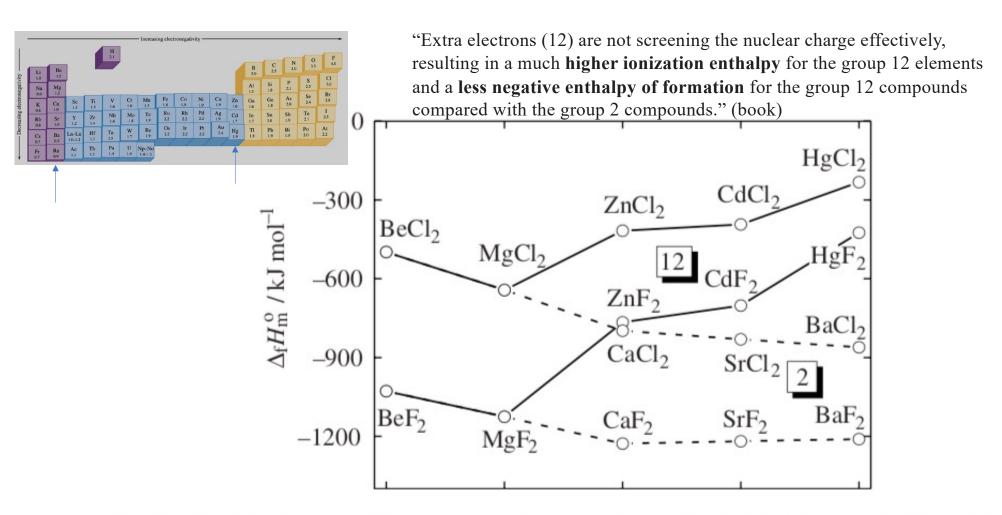


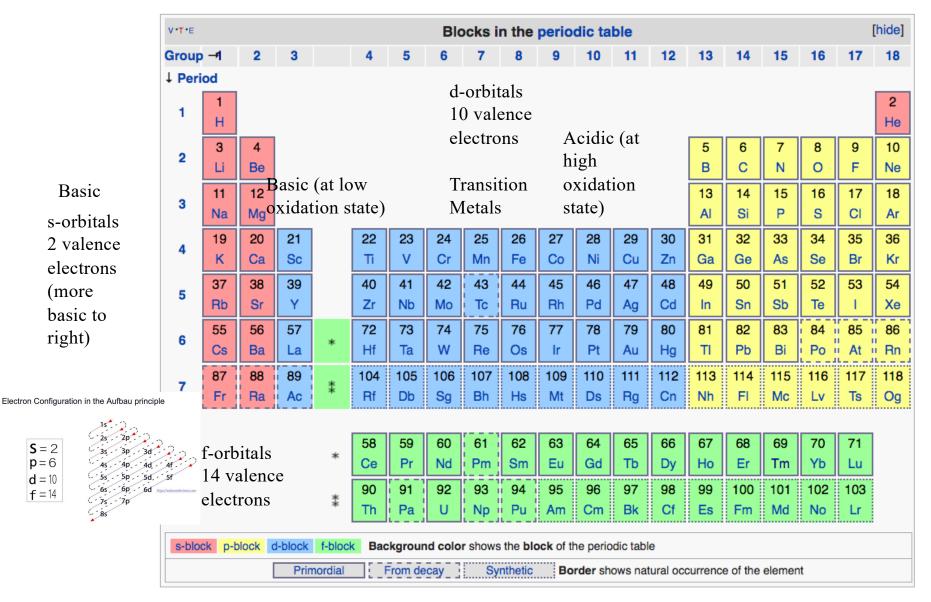
Figure 7.6 Enthalpy of formation of group 2 and 12 dichlorides and difluorides.

Transition Metal Enthalpy of Formation

$$\Delta_{\text{latt}}H_{\text{m}} = \Phi_{\text{electrostatic}} + \Phi_{\text{repulsion}} + \Phi_{\text{dispersion}} + \Phi_{\text{polarization}} + \Phi_{\text{crystal field}}$$

Crystal Field Theory (CFT):

This theory explains how the arrangement of ligands around a central metal ion splits the d orbitals into different energy levels, depending on the geometry of the complex.



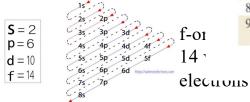
Acidic

p-orbitals 6 valence electrons (more acidic to right)

Hybridization schemes for the σ -bonding frameworks of different geometrical configurations

Coordination number	Arrangement of donor atoms	Orbitals hybridized	Hybrid orbital description	Example
2	Linear	s, p_z	sp	$[Ag(NH_3)_2]^+$
3	Trigonal planar	s, p_x, p_y	sp^2	$[HgI_3]^-$
4	Tetrahedral	s, p_x, p_y, p_z	sp^3	$[FeBr_4]^{2-}$
4	Square planar	$s, p_x, p_y, d_{x^2-y^2}$	sp^2d	$[Ni(CN)_4]^{2-}$
5	Trigonal bipyramidal	$s, p_x, p_y, p_z, d_{z^2}$	sp^3d	[CuCl ₅] ³⁻
5	Square-based pyramidal	$s, p_x, p_y, p_z, d_{x^2-y^2}$	sp^3d	$[Ni(CN)_5]^{3-}$
6	Octahedral	$s, p_x, p_y, p_z, d_{z^2}, d_{x^2-y^2}$	sp^3d^2	$[Co(NH_3)_6]^{3+}$
6	Trigonal prismatic	s, d_{xy} , d_{yz} , d_{xz} , d_{z^2} , $d_{x^2-y^2}$ or s, p_x , p_y , p_z , d_{xz} , d_{yz}	sd^5 or sp^3d^2	$[ZrMe_6]^{2-}$
7	Pentagonal bipyramidal	$s, p_x, p_y, p_z, d_{xy}, d_{x^2-y^2}, d_{z^2}$	sp^3d^3	$[V(CN)_7]^{4-}$
7	Monocapped trigonal prismatic	$s, p_x, p_y, p_z, d_{xy}, d_{xz}, d_{z^2}$	sp^3d^3	[NbF ₇] ²⁻
8	Cubic	$s, p_x, p_y, p_z, d_{xy}, d_{xz}, d_{yz}, f_{xyz}$	sp^3d^3f	[PaF ₈] ³⁻
8	Dodecahedral	$s, p_x, p_y, p_z, d_{z^2}, d_{xy}, d_{xz}, d_{yz}$	sp^3d^4	$[Mo(CN)_8]^{4-}$
8	Square antiprismatic	$s, p_x, p_y, p_z, d_{xy}, d_{xz}, d_{yz}, d_{x^2-y^2}$	sp^3d^4	$[TaF_8]^{3-}$
9	Tricapped trigonal	$s, p_x, p_y, p_z, d_{xy}, d_{xz}, d_{yz}, d_{z^2}, d_{z^2}, d_{x^2-y^2}$	sp^3d^5	$[ReH_9]^{2-}$

Electron Configuration in the Aufbau principle



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Crystal Field Theory

$$E \propto \frac{q_1 q_2}{r}$$

- E the bond energy between the charges and
- q₁ and q₂ are the charges of the interacting ions and
- r is the distance separating them.

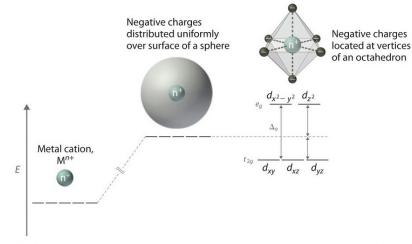
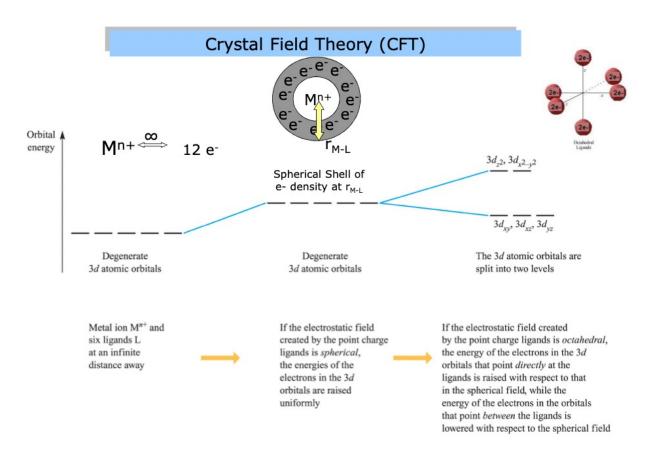


Figure 1: Distributing a charge of -6 uniformly over a spherical surface surrounding a metal ion causes the energy of all five d orbitals to increase due to electrostatic repulsions, but the five d orbitals remain degenerate. Placing a charge of -1 at each vertex of an octahedron causes the d orbitals to split into two groups with different energies: the $d_{x^2-y^2}$ and d_{z^2} orbitals increase in energy, while the, d_{xy} , d_{xz} , and d_{yz} orbitals decrease in energy. The average energy of the five d orbitals is the same as for a spherical distribution of a -6 charge, however. Attractive electrostatic interactions between the negatively charged ligands and the positively charged metal ion (far right) cause all five d orbitals to decrease in energy but does not affect the splittings of the orbitals. The two e_g orbitals point directly at the six negatively charged ligands, which increases their energy compared with a spherical distribution of negative charge. In contrast, the three t_{2g} orbitals point between the negatively charged ligands, which decreases their energy compared with a spherical distribution of charge.

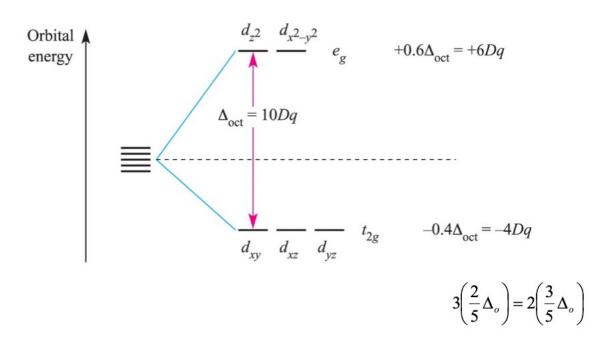
larger the splitting. Ligands are classified as strong or weak based on the spectrochemical series:

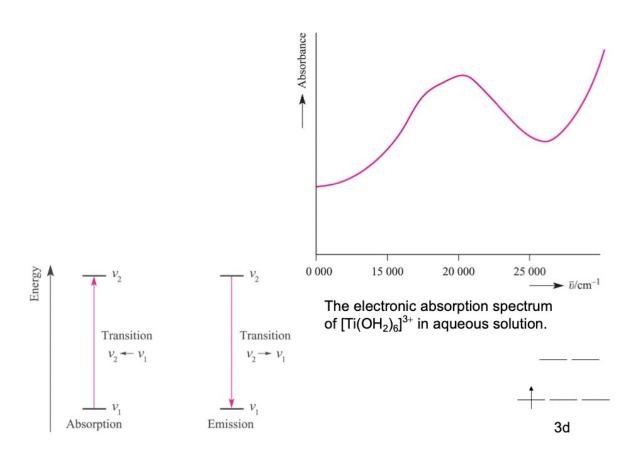
$$I^- < Br^- < Cl^- < SCN^- < F^- < OH^- < ox^{2-} < ONO^- < H_2O < SCN^- < EDTA^{4-} < NH_3 < en < NO_2^- < CN^-$$

Note that SCN⁻ and NO₂- ligands are represented twice in the above spectrochemical series since there are two different Lewis base sites (e.g., free electron pairs to share) on each ligand (e.g., for the SCN⁻ ligand, the electron pair on the sulfur or the nitrogen can form the coordinate covalent bond to a metal). The specific atom that binds in such ligands is underlined.



Crystal Field Stabilization Energy (CFSE)





Complex	Δ/cm^{-1}	Complex	Δ/cm^{-1}
$[TiF_6]^{3-}$	17 000	$[Fe(ox)_3]^{3-}$	14 100
$[Ti(OH_2)_6]^{3+}$	20 300	$[Fe(CN)_6]^{3-}$	35 000
$[V(OH_2)_6]^{3+}$	17850	$[Fe(CN)_6]^{4-}$	33 800
$[V(OH_2)_6]^{2+}$	12 400	$[CoF_6]^{3-}$	13 100
$[CrF_6]^{3-}$	15 000	$[Co(NH_3)_6]^{3+}$	22 900
$[Cr(OH_2)_6]^{3+}$	17 400	$[Co(NH_3)_6]^{2+}$	10 200
$[Cr(OH_2)_6]^{2+}$	14 100	$[Co(en)_3]^{3+}$	24 000
$[Cr(NH_3)_6]^{3+}$	21 600	$[Co(OH_2)_6]^{3+}$	18 200
$[Cr(CN)_{6}]^{3-}$	26 600	$[Co(OH_2)_6]^{2+}$	9 300
$[MnF_6]^{2-}$	21 800	$[Ni(OH_2)_6]^{2+}$	8 500
$[Fe(OH_2)_6]^{3+}$	13 700	$[Ni(NH_3)_6]^{2+}$	10 800
$[Fe(OH_2)_6]^{2+}$	9 400	$[Ni(en)_3]^{2+}$	11 500

Values of $\Delta_{\rm oct}$ for some $\emph{d}\text{-block}$ metal complexes.

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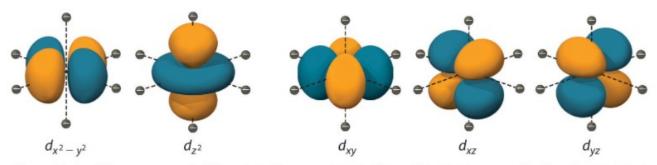


Figure 3: Spatial arrangement of ligands in the an octahedral ligand field with respect to the five d-orbitals.

- d_{xy}: lobes lie in-between the x and the y axes.
- d_{xz}: lobes lie in-between the x and the z axes.
- d_{yz}: lobes lie in-between the y and the z axes.
- d_{x²-v²}: lobes lie on the x and y axes.
- d_z²: there are two lobes on the z axes and there is a donut shape ring that lies on the xy plane around the other two lobes.

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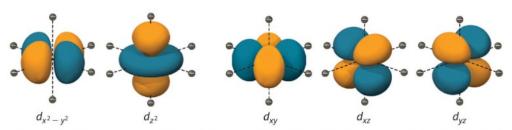


Figure 3: Spatial arrangement of ligands in the an octahedral ligand field with respect to the five d-orbitals.

Octahedral Complexes

In an octahedral complex, there are six ligands attached to the central transition metal. The d-orbital splits into two different levels (Figure 4). The bottom three energy levels are named d_{xy} , d_{xz} , and d_{yz} (collectively referred to as e_g). The two upper energy levels are named $d_{x^2-y^2}$, and d_{z^2} (collectively referred to as e_g).

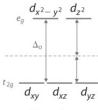
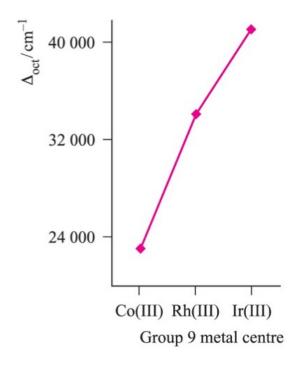


Figure 4.

The reason they split is because of the electrostatic interactions between the electrons of the ligand and the lobes of the d-orbital. In an octahedral, the electrons are attracted to the axes. Any orbital that has a lobe on the axes moves to a higher energy level. This means that in an octahedral, the energy levels of e_g are higher $(0.6\Delta_0)$ while t_{2g} is lower $(0.4\Delta_0)$. The distance that the electrons have to move from t_{2g} from e_g and it dictates the energy that the complex will absorb from white light, which will determine the color. Whether the complex is paramagnetic or diamagnetic will be determined by the spin state. If there are unpaired electrons, the complex is paramagnetic; if all electrons are paired, the complex is diamagnetic.



The trend in values of Δ_{oct} for the complexes $[M(NH_3)_6]^{3+}$ where M = Co, Rh, Ir.

Field strength increases as one proceeds down a column.

$$\mathsf{Mn}(\mathsf{II}) < \mathsf{Ni}(\mathsf{II}) < \mathsf{Co}(\mathsf{II}) < \mathsf{Fe}(\mathsf{II}) < \mathsf{Cr}(\mathsf{III}) < \mathsf{Co}(\mathsf{III}) < \mathsf{Ru}(\mathsf{III}) < \mathsf{Mo}(\mathsf{III}) < \mathsf{Rh}(\mathsf{III}) < \mathsf{Pd}(\mathsf{II}) < \mathsf{Pt}(\mathsf{IV})$$

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Complex	Δ/cm^{-1}	Complex	Δ/cm^{-1}
$[TiF_6]^{3-}$	17 000	$[Fe(ox)_3]^{3-}$	14 100
$\left[\mathrm{Ti}(\mathrm{OH_2})_6\right]^{3+}$	20 300	$[Fe(CN)_6]^{3-}$	35 000
$[V(OH_2)_6]^{3+}$	17850	$[Fe(CN)_6]^{4-}$	33 800
$[V(OH_2)_6]^{2+}$	12 400	$[CoF_{6}]^{3-}$	13 100
$[CrF_6]^{3-}$	15 000	$[Co(NH_3)_6]^{3+}$	22 900
$[Cr(OH_2)_6]^{3+}$	17 400	$[Co(NH_3)_6]^{2+}$	10 200
$[Cr(OH_2)_6]^{2+}$	14 100	$[Co(en)_3]^{3+}$	24 000
$[Cr(NH_3)_6]^{3+}$	21 600	$[Co(OH_2)_6]^{3+}$	18 200
$[Cr(CN)_6]^{3-}$	26 600	$[Co(OH_2)_6]^{2+}$	9 300
$[MnF_6]^{2-}$	21 800	$[Ni(OH_2)_6]^{2+}$	8 500
$[Fe(OH_2)_6]^{3+}$	13 700	$[Ni(NH_3)_6]^{2+}$	10 800
$[Fe(OH_2)_6]^{2+}$	9 400	$[Ni(en)_3]^{2+}$	11 500

Values of $\Delta_{\rm oct}$ for some $\emph{d}\text{-block}$ metal complexes.

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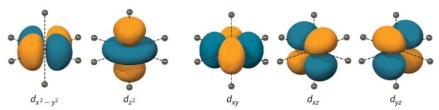


Figure 3: Spatial arrangement of ligands in the an octahedral ligand field with respect to the five d-orbitals.

Tetrahedral Complexes

In a tetrahedral complex, there are four ligands attached to the central metal. The d orbitals also split into two different energy levels. The top three consist of the d_{xy} , d_{xz} , and d_{yz} orbitals. The bottom two consist of the $d_{x^2-y^2}$ and d_{z^2} orbitals. The reason for this is due to poor orbital overlap between the metal and the ligand orbitals. The orbitals are directed on the axes, while the ligands are not.

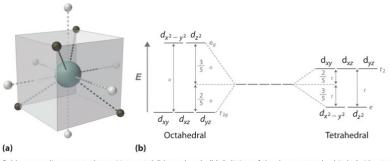


Figure 5: (a) Tetraheral ligand field surrounding a central transition metal (blue sphere). (b) Splitting of the degenerate d-orbitals (without a ligand field) due to an octahedral ligand field (left diagram) and the tetrahedral field (right diagram).

The difference in the splitting energy is tetrahedral splitting constant (Δ_t) , which less than (Δ_o) for the same ligands:

$$\Delta_t = 0.44 \, \Delta_o \tag{2}$$

Consequentially, Δ_t is typically smaller than the spin pairing energy, so tetrahedral complexes are usually **high spin**.

https://chem.libretexts.org/Bookshelves/Inorganic_Chemistry/Supplemental_Modules_and_Web sites (Inorganic Chemistry)/Crystal Field Theory/Crystal Field Theory

Spin Pairing Energy

•The energy needed to pair two electrons in the same orbital, overcoming the natural tendency for electrons to occupy different orbitals with parallel spins (Hund's rule).

•Impact on complex behavior:

•When considering transition metal complexes, the relative magnitude of the spin pairing energy compared to the crystal field splitting energy determines whether a complex will be "high spin" (with many unpaired electrons) or "low spin" (with more paired electrons).

•Paramagnetism and diamagnetism:

•If a complex has unpaired electrons (high spin), it will be paramagnetic, meaning it will be attracted to a magnetic field; if all electrons are paired (low spin), it will be diamagnetic, repelled by a magnetic field.

https://chem.libretexts.org/Bookshelves/Inorganic_Chemistry/Supplemental_Modules_and_Web sites (Inorganic Chemistry)/Crystal Field Theory/Crystal Field Theory

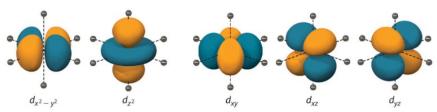


Figure 3: Spatial arrangement of ligands in the an octahedral ligand field with respect to the five d-orbitals.

Square Planar Complexes

In a square planar, there are four ligands as well. However, the difference is that the electrons of the ligands are only attracted to the xy plane. Any orbital in the xy plane has a higher energy level (Figure 6). There are four different energy levels for the square planar (from the highest energy level to the lowest energy level): $d_{x^2-y^2}$, d_{xy} , d_{z^2} , and both d_{xz} and d_{yz} .

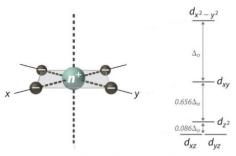


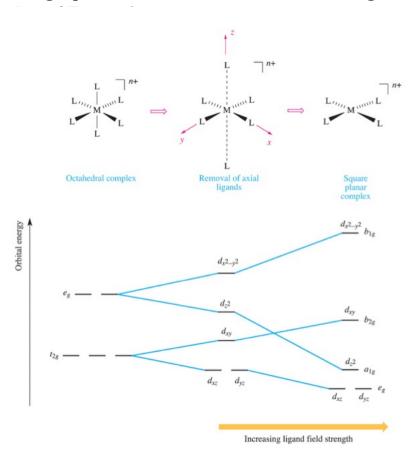
Figure 6: Splitting of the degenerate d-orbitals (without a ligand field) due to an square planar ligand field.

The splitting energy (from highest orbital to lowest orbital) is Δ_{sp} and tends to be larger then Δ_o

$$\Delta_{sp} = 1.74 \, \Delta_o \tag{3}$$

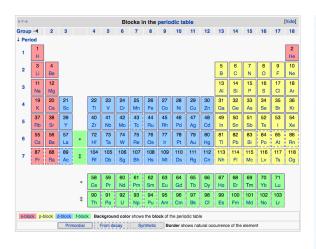
Moreover, Δ_{sp} is also larger than the pairing energy, so the square planar complexes are usually **low spin** complexes.

Square Planar



Depending on the crystallographic environment the d-orbital energies split This impacts the Enthalpy of Formation

 $https://chem.libretexts.org/Bookshelves/Inorganic_Chemistry/Supplemental_Modules_and_Websites_(Inorganic_Chemistry)/Crystal_Field_Theory/Crystal_Field_Theory$



Electron Configuration in the Aufbau principle

For the complex ion $[Fe(Cl)_6]^{3}$ determine the number of d electrons for Fe, sketch the d-orbital energy levels and the distribution of d electrons among them, list the number of lone electrons, and label whether the complex is paramagnetic or diamagnetic.

Solution

- Step 1: Determine the oxidation state of Fe. Here it is Fe³⁺. Based on its electron configuration, Fe³⁺ has **5 d-electrons**.
- Step 2: Determine the geometry of the ion. Here it is an octahedral which means the energy splitting should look like:

$$e_{g} \xrightarrow{d_{X^{2}-y^{2}}} \xrightarrow{d_{z^{2}}} \xrightarrow{d_{z^{2}}}$$

$$\downarrow t_{2g} \xrightarrow{d_{xy}} \xrightarrow{d_{xz}} \xrightarrow{d_{yz}}$$

• Step 3: Determine whether the ligand induces is a strong or weak field spin by looking at the spectrochemical series. Cl⁻ is a weak field ligand (i.e., it induces high spin complexes). Therefore, electrons fill all orbitals before being paired.

- Step four: Count the number of lone electrons. Here, there are 5 electrons.
- Step five: The five unpaired electrons means this complex ion is paramagnetic (and strongly so).

Depending on the crystallographic environment the d-orbital energies split This impacts the Enthalpy of Formation

https://chem.libretexts.org/Bookshelves/Inorganic_Chemistry/Supplemental_Modules_and_Websites (Inorganic Chemistry)/Crystal Field Theory/Crystal Field Theory

A tetrahedral complex absorbs at 545 nm. What is the respective octahedral crystal field splitting (Δ_o) ? What is the color of the complex?

Solution

$$\Delta_t = \frac{hc}{\lambda}$$

$$= \frac{(6.626 \times 10^{-34} J \cdot s)(3 \times 10^8 m/s)}{545 \times 10^{-9} m}$$

$$= 3.65 \times 10^{-19} J$$

However, the *tetrahedral* splitting (Δ_t) is ~4/9 that of the *octahedral* splitting (Δ_o).

$$\Delta_t = 0.44 \Delta_o$$

$$\Delta_o = \frac{\Delta_t}{0.44}$$

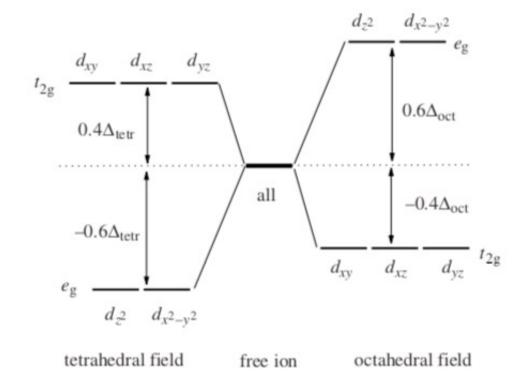
$$= \frac{3.65 \times 10^{-19} J}{0.44}$$

$$= 8.30 \times 10^{-18} J$$

This is the energy needed to promote *one* electron in *one* complex. Often the crystal field splitting is given per mole, which requires this number to be multiplied by Avogadro's Number (6.022×10^{23}) .

This complex appears red, since it absorbs in the complementary green color (determined via the color wheel).

Depending on the crystallographic environment the d-orbital energies split This impacts the Enthalpy of Formation



Crystal Field Effect

Figure 7.8 d level splitting for octahedral and tetrahedral crystal fields.

Crystal Field Stabilization Energy

Factors affecting the CFSE

First, note that the pairing energies for first-row transition metals are relatively constant.

Therefore, the difference between strong- and weak-field, or low and high- spin cases comes down to the magnitude of the crystal field splitting energy (Δ).

1. Geometry is one factor, Δ_0 is larger than Δ_t

In almost all cases, the Δ_t is smaller than P (pairing energy), so...

Tetrahedral complexes are always weak-field (high spin)

Square planar complexes may either be weak- or strong-field.

2. Oxidation State of Metal Cation -

A greater charge on cation results in a greater magnitude of Δ

Why? A greater charge pulls ligands more strongly towards the metal, therefore influences the splitting of the energy levels more.

3. Size of the Metal Cation -

For second and third-row transition metal ions, Δ_0 is larger than first-row.

Less steric hindrance between the ligands – better overlap w/orbitals.

Crystal Field Stabilization Energy

4. Identity of the ligands.

A spectrochemical series has been developed and sorted by the ability to split metal d-orbitals.

```
I^- < Br^- < S^{2-} < Cl^- < SCN^- < NO_3^- < N^{3-} < F^- < OH^- < C_2O_4^{2-} < H_2O < NCS^- < CH_3CN < py (pyridine) < NH_3 < en (ethylenediamine) < bipy (2,2'-bipyridine) < <math>NO_2^- < PPh_3 < CN^- < CO
```

As the ligands decrease in size, their ability to split the d-orbitals increases. The larger and bulkier ligands exhibit more steric hindrance and approach the metal less effectively.

One might expect that ligands with a negative charge might split the d-orbitals better, but this is not always the case. Notice that water is higher in the series than OH⁻, even though O on OH⁻ has a high concentration of charge.

The dipole moment of H_2O is larger than NH_3 , but NH_3 is higher in the series. PPh_3 is high in the series, but also very bulky, neutral and has a small dipole moment.

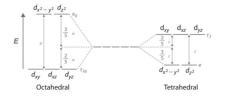
Transition metal lattice stabilization due to d-orbital splitting

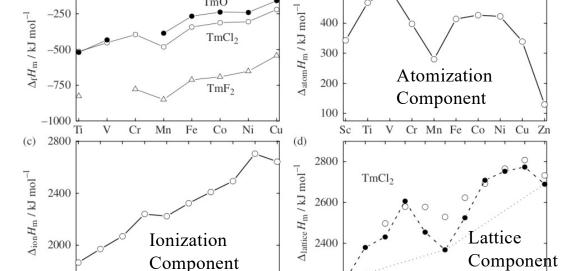
(a)

 $\Delta_{f}H_{m}(MX) = -\Delta_{latt}H_{m} + \Delta_{atom}H_{m} + \Delta_{ion}H_{m} + \Delta_{diss}H_{m} + \Delta_{eg}H_{m}$

V Cr Mn Fe Co Ni Cu Zn

First series chlorides, oxides and fluorides Increasing d electrons





TmO

Cr Mn Fe Co Ni Cu Zn

500

Crystal Field Stabilization due to dorbital splitting (not for Ca, Mn, Zn)

Figure 7.9 Thermodynamic data (b)–(d) needed in analysis of the enthalpy of formation of the binary transition metal compounds given in (a). (b) Atomization enthalpy of first series transition metals; (c) sum of first and second ionization enthalpies of first series transition metals; (d) derived lattice enthalpy of transition metal dihalides.

2200

Ca Sc Ti

Heat of Formation for Transition Metal Oxides in Different Oxidation States

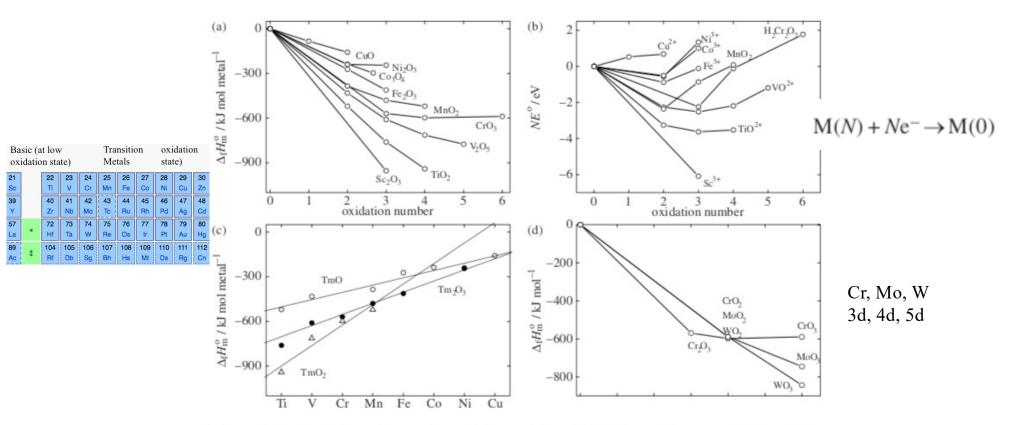


Figure 7.11 Enthalpy of formation of binary oxides of the 3d transition metals (a) and (c), Frost diagram for the same 3d metals (b) Enthalpy of formation of binary oxides of the group 6 transition metals.

Acid-Base Model for Heat of Formation of Ternary Oxides

$$AO + B_xO_y = AB_xO_{1+y}$$

SiO₂

Acid

accepts

oxygen

p-block

oxides

Basicity

MgO < CaO < SrO < BaO

Na₂O Base

transfers its oxygen s-block

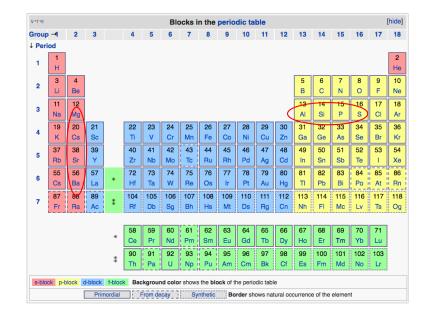
oxides

SiO₄²⁻

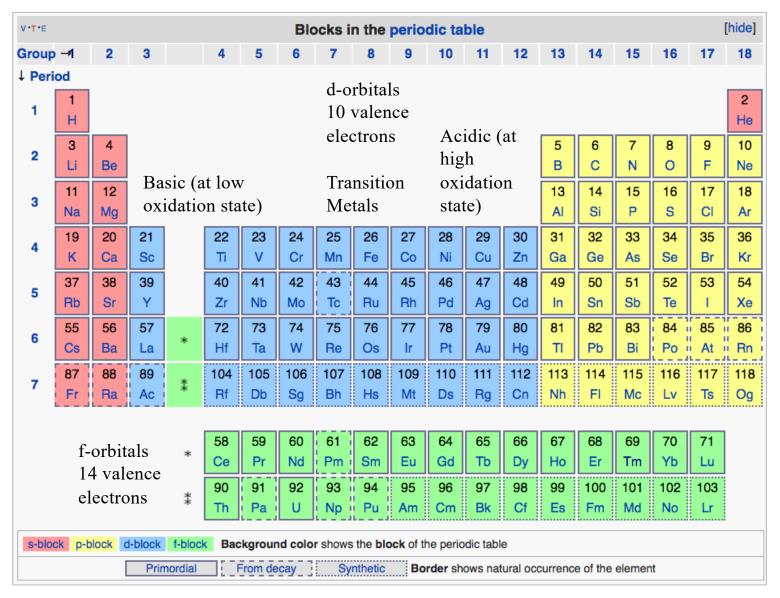
SiNa₂O₃

Acidity

A1 < Si < P < S



Basic s-orbitals 2 valence electrons (more basic to right)



p-orbitals 6 valence electrons (more acidic to right)

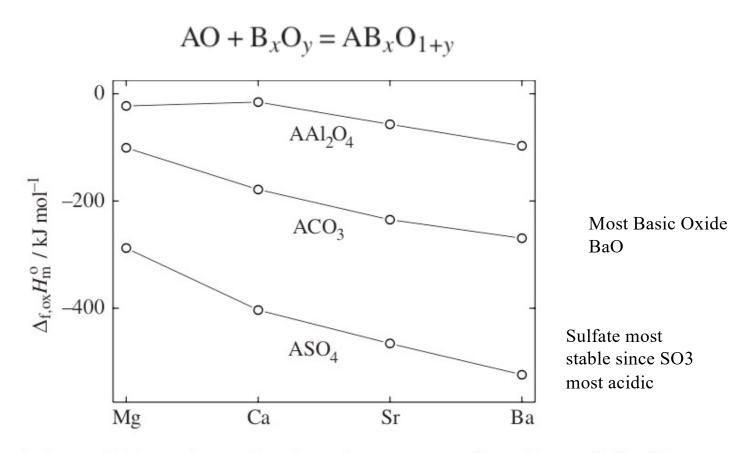


Figure 7.14 Enthalpy of formation of selected ternary oxides from their binary constituents.

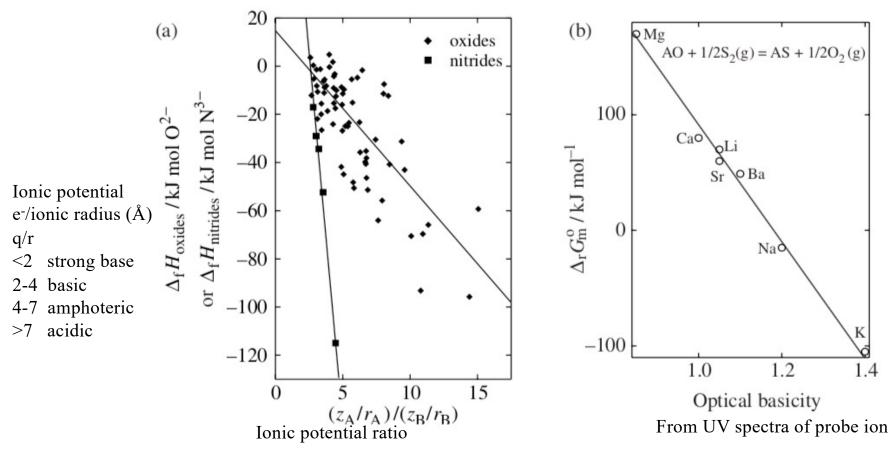
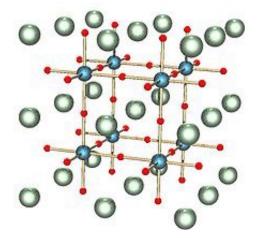


Figure 7.15 (a) Enthalpy of formation of ternary oxides and nitrides from their binary constituent compounds as a function of the ratio of ionic potential [16]. Reprinted with permission from [16] Copyright (1997) American Chemical Society. (b) Gibbs energy of the oxide–sulfide equilibrium for group 1 and 2 metals at 1773 K as a function of the optical basicity of the metal.

Atomic Size

Perovskite structure
Calcium titanate CaTiO₃
Embed cations in the structure for engineered properties
One is solar energy absorption in Graetzel cells
These are the most promising low-temperature formation PV devices
(silicon solar cells require high temperature reduction of silica and chemical purification)

Red O²⁻ Blue Ti⁴⁺ Green Ca²⁺ or Ba²⁺



 $\label{lem:cubic-orthonombic-like} Cubic/Orthorhombic-like structure \\ Can accommodate many transition metals \\ ABX_3$

A is much larger than B cations, X is anion (oxide) B has 6-fold coordination surrounded by octahedron of anions
A has 12-fold cubahedral coordination

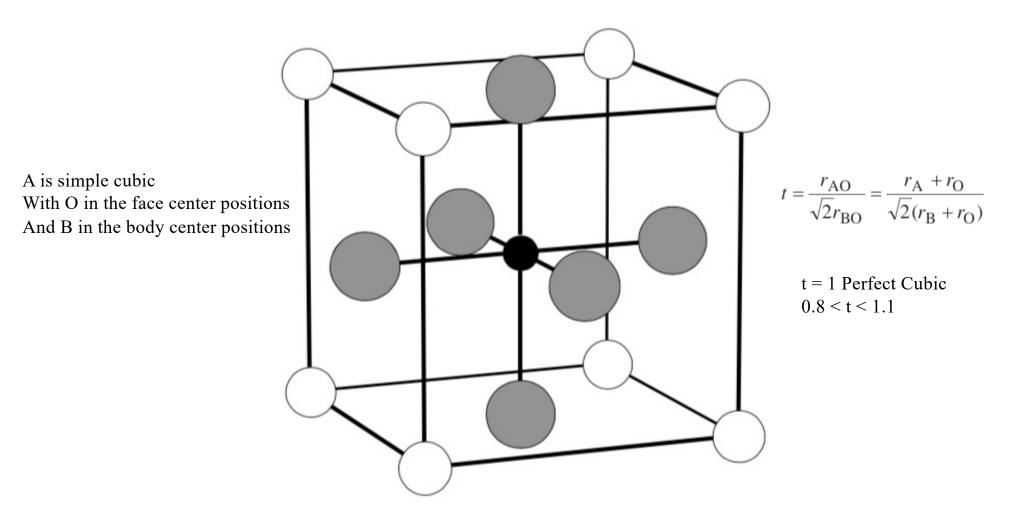


Figure 7.16 The perovskite-type structure. Small black circles represent the B atom, large grey circles represent O atoms and open circles represent the A atom.

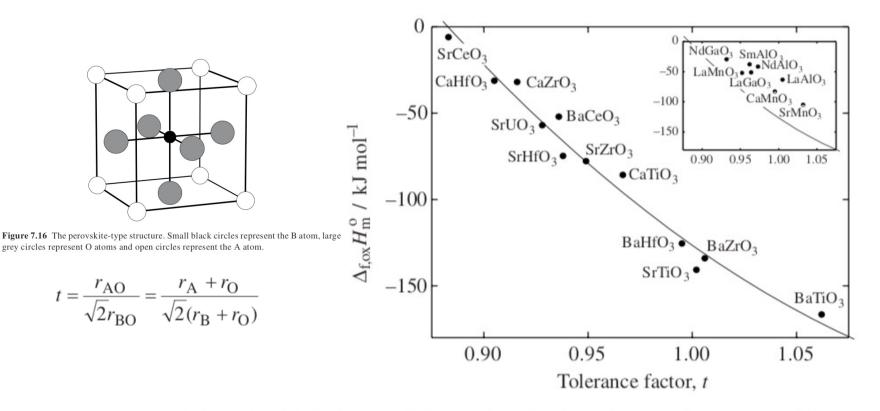
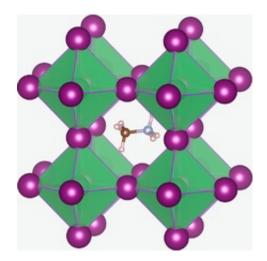


Figure 7.17 Enthalpy of formation of selected perovskite-type oxides as a function of the tolerance factor. Main figure show data for perovskites where the A atom is a Group 2 element and B is a *d* or *f* element that readily takes a tetravalent state [19, 20]. The insert shows enthalpies of formation of perovskite-type oxides where the A atom is a trivalent lanthanide metal [21] or a divalent alkaline earth metal [22] whereas the B atom is a late transition metal atom or Ga/Al.

Methyl Ammonium Lead Halide



Schematic of a sensitized perovskite solar cell in which the active layer consist of a layer of mesoporous TiO2 which is coated with the perovskite absorber. The active layer is contacted with an n-type material for electron extraction and a p-type material for hole extraction. b) Schematic of a thinfilm perovskite solar cell. In this architecture in which just a flat layer of perovskite is sandwiched between two selective contacts. c) Charge generation and extraction in the sensitized architecture. After light absorption in the perovskite absorber the photogenerated electron is injected into the mesoporous TiO₂ through which it is extracted. The concomitantly generated hole is transferred to the p-type material. d) Charge generation and extraction in the thin-film architecture. After light absorption both charge generation as well as charge extraction occurs in the perovskite layer.

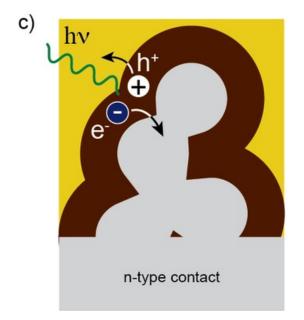
Sensitized perovskite solar cell

p-type contact

mp-TiO, + perovskite

n-type contact

anode



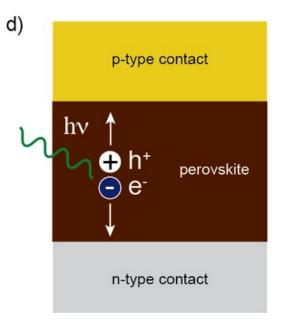
Thin-film perovskite solar cell

p-type contact

perovskite

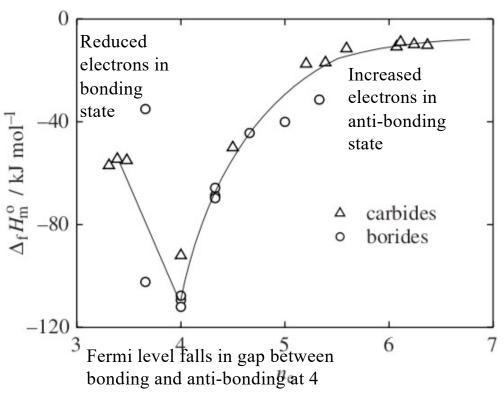
n-type contact

anode



spiro Ometad p-type semi-conductor

Enthalpy of Formation versus Number of Valence Electrons



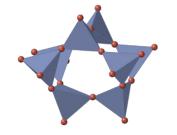
TiC with ne = 4 has a high enthalpy of formation since the Fermi level falls in a pronounced gap in density of electronic states separating bonding and antibonding electron bands.

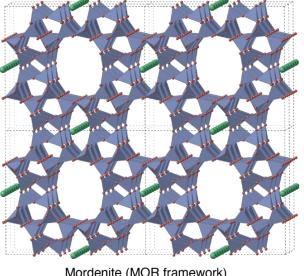
Figure 7.18 Enthalpy of formation of binary carbides and diborides [25, 26] as a function of the average number of valence electrons per atom.

Zeolites (Natural are aluminosilicate rocks, synthetic can be a variety of materials often based on SiO₂)



secondary building unit (cage)





Mordenite (MOR framework)

Microscopic structure of a zeolite (mordenite) framework, assembled from tetrahedra. Sodium is present as an extra-framework cation (in green).

Can form meso or micro pores (colloidal- or nano-scale) (These are terms from gas adsorption field.)

Reference 29

Synthetic Zeolites can have meso (colloidal) or micro (nano) pores depending on the templating material and synthesis conditions. Usually start with TEOS and a surfactant or block copolymer

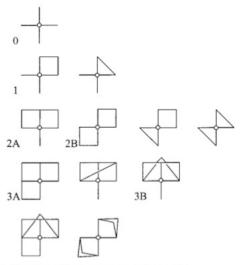
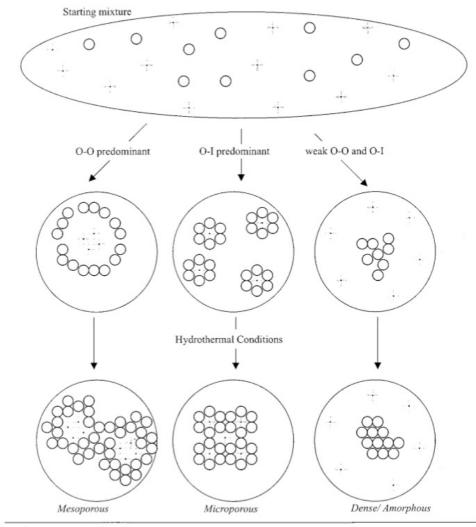


Figure 5. Configuration loops present in zeolites.



- O Inorganic (silicate) species
- · Organic (SDA) species

Figure 1. Possibilities for silicate self-assembly in hydrothermal syntheses.

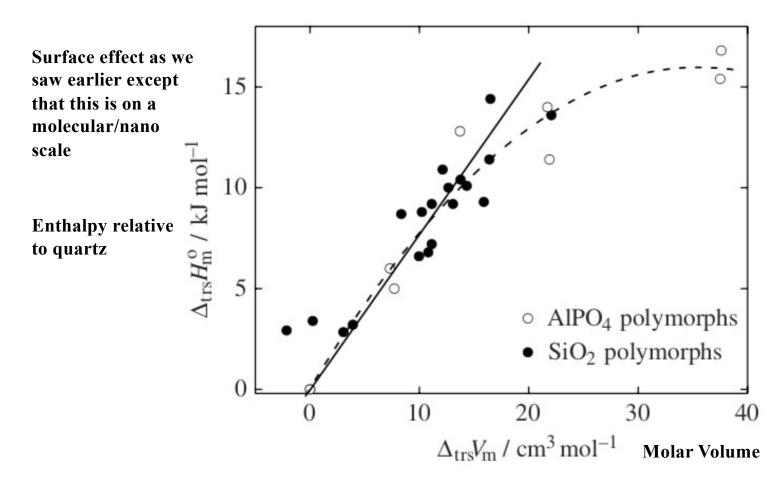


Figure 7.19 Enthalpy of transition from the stable polymorph versus volume correlations for micro- and mesoporous SiO₂ and AlPO₄ materials [29, 34].

Energy of Formation for Substitutional Solid Solutions

Atomic Radii => Volume of compounds

Hume-Rothery Rule limited solubility if size difference exceeds 15% Electronegativity

Large difference in binary system leads to negative enthalpy of mixing Pd-Zr and is small for systems with low or no electronegativity and size difference Ti-Zr

Valence electron density

Binary components have the same crystal structure

Large enthalpy of mixing is related to large number of intermetallic phases

Elastic contribution to the enthalpy of mixing, small mixes well with large

$$\Delta_{\text{mix}} H_{\text{m}} = x_{\text{A}} x_{\text{B}}^2 c_{\text{A}} \frac{\Delta V^2}{3V_{\text{A}}} + x_{\text{B}} x_{\text{A}}^2 c_{\text{B}} \frac{\Delta V^2}{3V_{\text{B}}}$$

 c_i are constants x_i mole fractions V molar volumes Sub-regular solution model

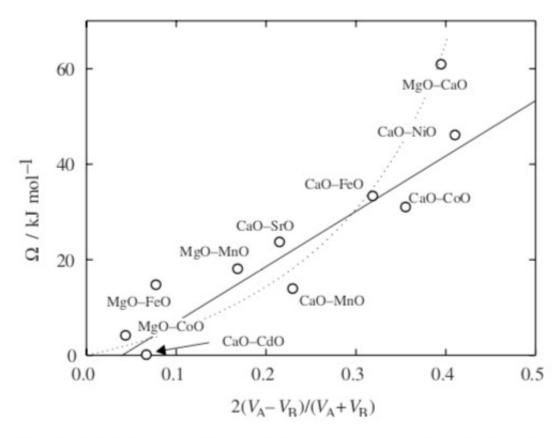


Figure 7.21 Enthalpies of mixing of selected NaCl-type systems involving the alkali earth oxides. The solid and dashed lines show scaling with the volume mismatch and with the square of the volume mismatch, respectively.

Energy of Formation for Interstitial Solid Solutions

Elastic interactions
Electronic interactions

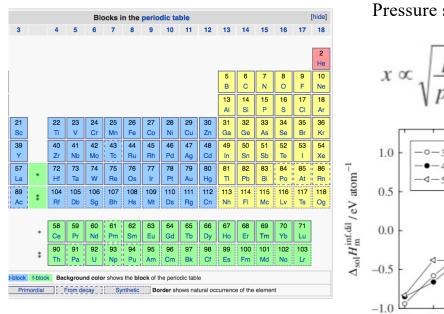
Gas solubility in metals

Temperature

Pressure solubility for $H_2 \times \sqrt{p}$ $M + \frac{x}{2}H_2(g) = MH_x$

$$x \propto \sqrt{\frac{p}{p_0}} \exp\left(\frac{\Delta_{7.22} S}{R}\right) \exp\left(\frac{\Delta_{7.22} H}{RT}\right)$$
 Sievert's Law

Solubility of gasses in metals



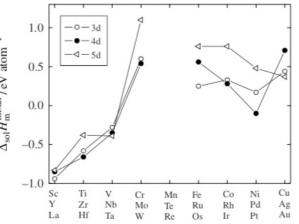


Figure 7.22 Enthalpy of solution of hydrogen in transition metals at infinite dilution [45].

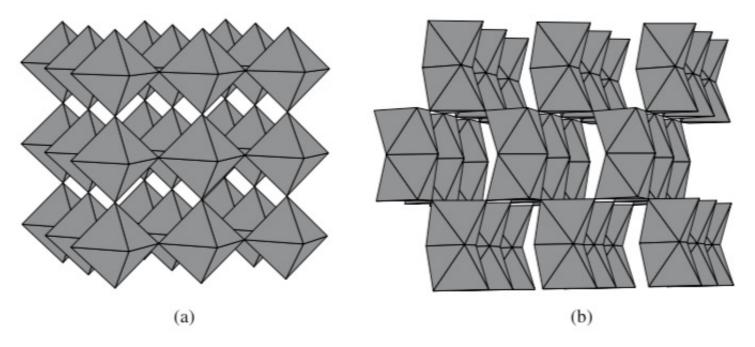


Figure 7.23 Connectivity of transition metal BO₆ octahedra in (a) cubic and (b) hexagonal perovskite SrMnO₃.

6 kJ/mole difference in formation enthalpy Reduction temperature is 600K higher for hexagonal Cubic reduced SrMnO_{2.5} is more stable Octahedral corners shared in cubic, faces shared in hexagonal High vacancies in faces make reduced hexagonal unfavorable

Liquid-Liquid Miscibility

Mixing of acidic (SiO₂) and Basic (CaO) oxides Si⁴⁺ has coordination number 4 and Ca²⁺ has 6 SiO₂ mixes well with CaO but CaO has a harder time mixing with SiO₂

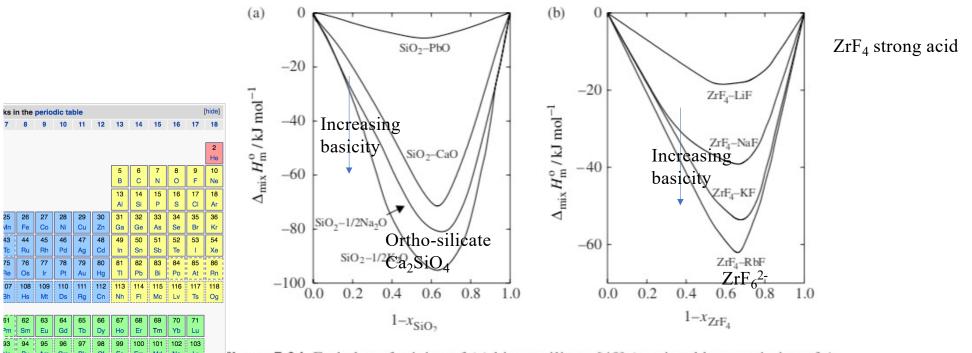


Figure 7.24 Enthalpy of mixing of (a) binary silicate [48] (reprinted by permission of A. Javrotsky) and (b) fluoride systems [49].

Liquid Salt Mixtures

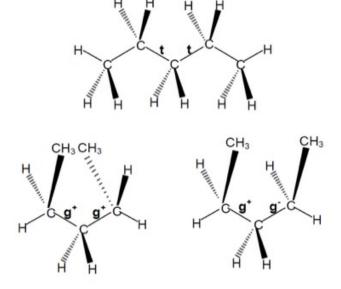
Size parameter, $d = (d_A - d_B)/(d_A + d_B)$

Common Anions mix with negative enthalpy of mixing Common cations do not mix due to anion-anion repulsion

The Rotational Isomeric State Model of Volkenstein and Paul Flory (Nobel Prize)

Carbon has a tetrahedral bonding arrangement For a chain of carbon, the two side groups interact with the side groups of neighboring carbons

For Butene



"Trans" is sterically the most favorable arrangement "Gauche +" and "Gauche -" are less favorable

The Boltzmann equation gives the probability of a particular conformation, **Z** is the partition function or the sum of all the different Boltzmann expressions in an ensemble

$$P(\varphi_i) = \frac{\exp(-E(\varphi_i)/kT)}{Z}$$

$$Z = \sum_{i} \mathrm{e}^{-\beta E_{i}}$$

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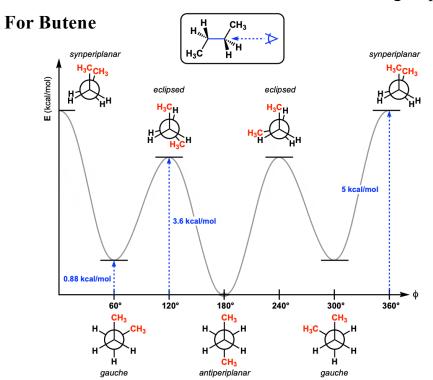
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Conformational Energy of Polymers

The Rotational Isomeric State Model of Volkenstein and Paul Flory (Nobel Prize)

Carbon has a tetrahedral bonding arrangement For a chain of carbon, the two side groups interact with the side groups of neighboring carbons

For Butene

$$Z = 1 + \exp\left(-E_{g^+}/kT\right) + \exp\left(-E_{g^-}/kT\right) = 1 + 2\sigma$$

$$Z = \sum_i \mathrm{e}^{-eta E_i}$$

Helmholtz Free Energy and Entropy

$$F_P = -kT \cdot \ln Z$$
; $S_P = -\frac{\partial F_P}{\partial T}$

$$P(\varphi_i) = \frac{\exp(-E(\varphi_i)/kT)}{Z}$$

Boltzmann equation where Z is number of states (which depend on temperature and energy barriers)

Internal Energy

$$\mathbf{U} = \mathbf{F_P} + \mathbf{S_PT}$$

$$^{-SUV}_{H \text{ A(F)}}$$

$$^{-pGT}$$

The Rotational Isomeric State Model of Volkenstein and Paul Flory (Nobel Prize)

For a polymer with N carbons there are N-2 covalent bonds

The number of discrete conformation states per chain is n^{N-2} where n is the number of discrete rotational states for the chain, tttt, $g^-g^-g^-g^-, g^+g^+g^+, g^+$ ttt, etc. for N = 4; $N_1 = 1$, $N_4 = 4$, etc. assuming no end effects

$$Z = \sum_{\{N_{\eta}\}} \frac{(N-2)!}{N_{1}! \dots N_{\nu}!} \exp(-N_{1}E(\varphi_{1})/kT) \dots \exp(-N_{\nu}E(\varphi_{\nu})/kT)$$

Average rotational angle

$$\langle \cos \varphi \rangle = \frac{\sum_{i=1}^{\nu} \exp(-E(\varphi_i)/kT) \cos \varphi_i}{\sum_{i=1}^{\nu} \exp(-E(\varphi_i)/kT)} = \frac{1-\sigma}{1+2\sigma}$$

Characteristic Ratio

$$C_{\infty} = \lim_{N \to \infty} \frac{\langle r^2 \rangle_0}{N l^2} = \frac{(1 + \cos \theta)}{(1 - \cos \theta)} \frac{(1 + \langle \cos \varphi \rangle)}{(1 - \langle \cos \varphi \rangle)}$$

$$\begin{aligned} & 180^{\circ} - 109^{\circ} = 71^{\circ} \\ & E_{g+} = 2100 \text{ J/mole} \\ & C_{\infty} = 3.6 \end{aligned}$$

$$\theta$$
 is the bond angle $180^{\circ}-109^{\circ} = 71^{\circ}$ $E_{g+} = 2100 \text{ J/mole}$ $C_{\infty} = 3.6$ Exp. 6.7